



PRIMES: Program for Research in Mathematics, Engineering and Science for High School Students

*In mathematics you don't understand things, you just get used to them.
- John von Neumann*



**Massachusetts
Institute of
Technology**

Institute for Medical Engineering and Sciences

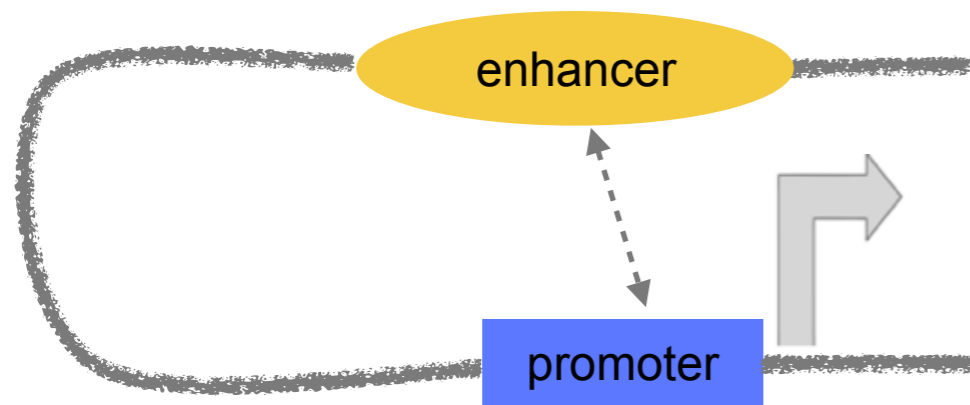
Chromatin organization: from polymer loops to topological domains

Boryana Doyle

Maxim Imakaev, Geoffrey Fudenberg,
Leonid Mirny

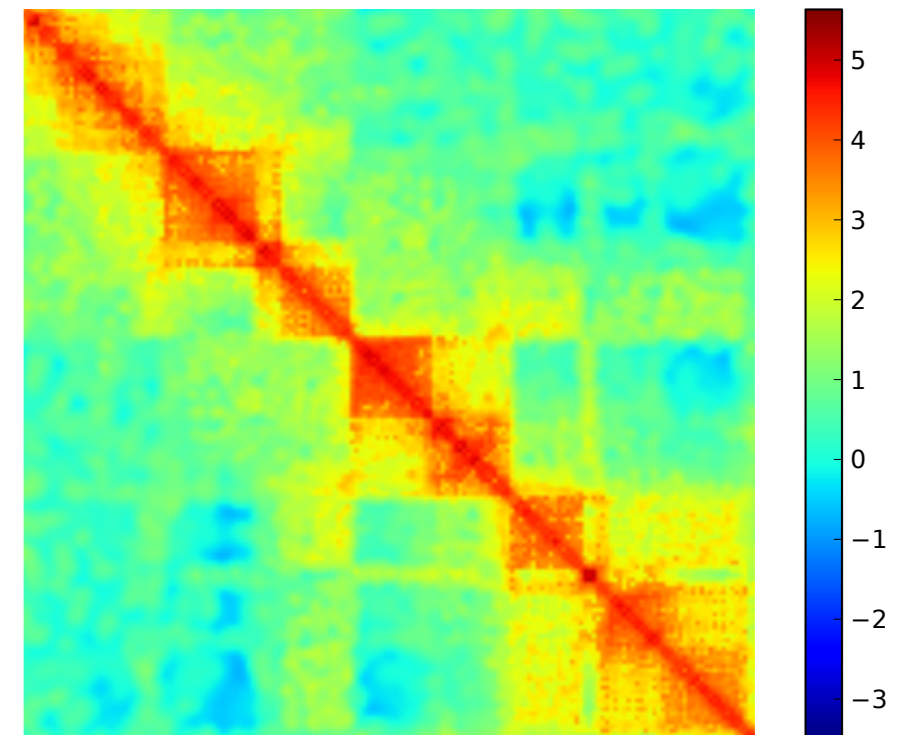
Outline

Part 1



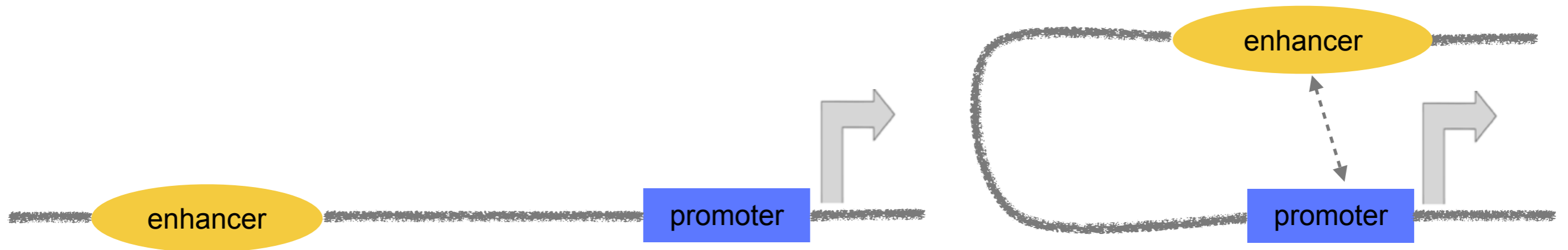
Enhancer-promoter interactions studied in polymer simulations

Part 2



Analysis of experimental Hi-C data

Part 1: Introduction

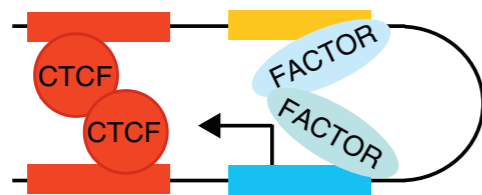


Current Opinion in Genetics & Development 2012, 22:79–85

Enhancer and promoter interactions—long distance calls

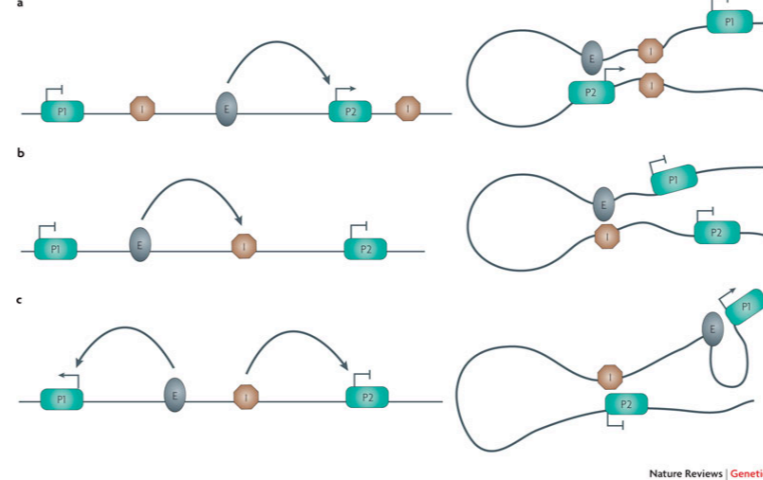
Ivan Krivega and Ann Dean

(a)



β -globin and APO

Raab and Kamakaka. Nat Rev Genet. 2010

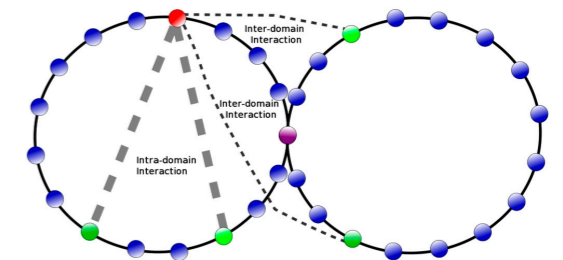


Nature Reviews | Genetics

PNAS | December 13, 2011 | vol. 108 | no. 50 | 19919–19924

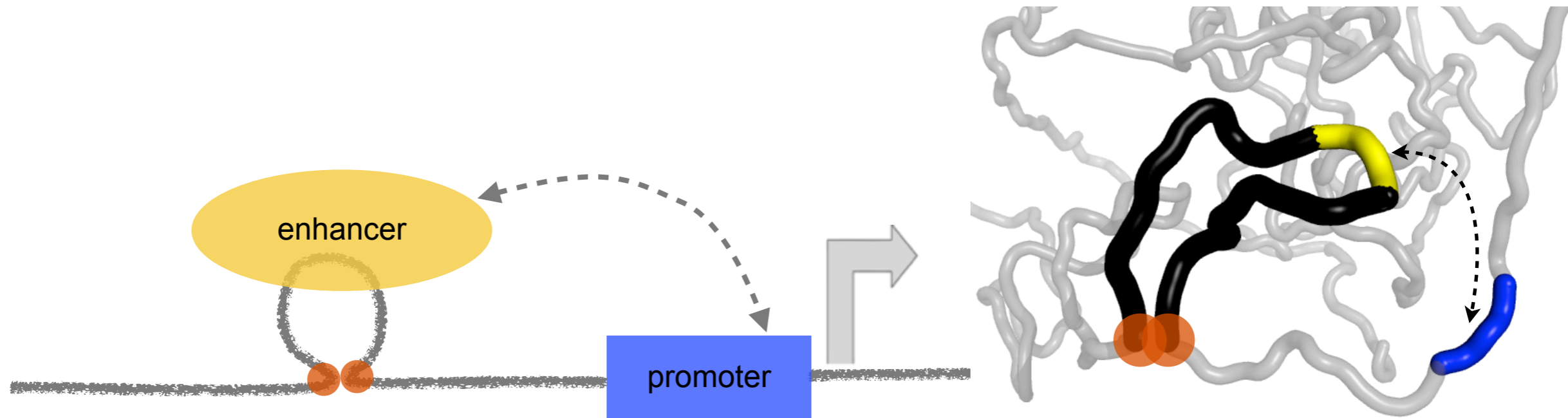
Theoretical analysis of the role of chromatin interactions in long-range action of enhancers and insulators

Swagatam Mukhopadhyay^a, Paul Schedl^b, Vasily M. Studitsky^{c,d}, and Anirvan M. Sengupta^{a,1}

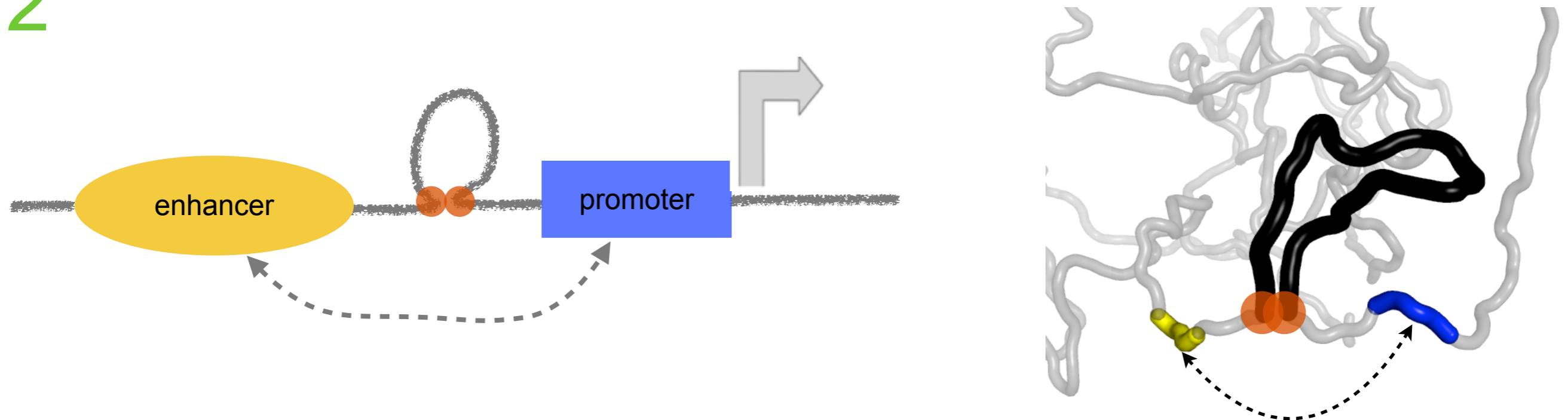


How can enhancer-promoter interactions be affected by local genome folding?

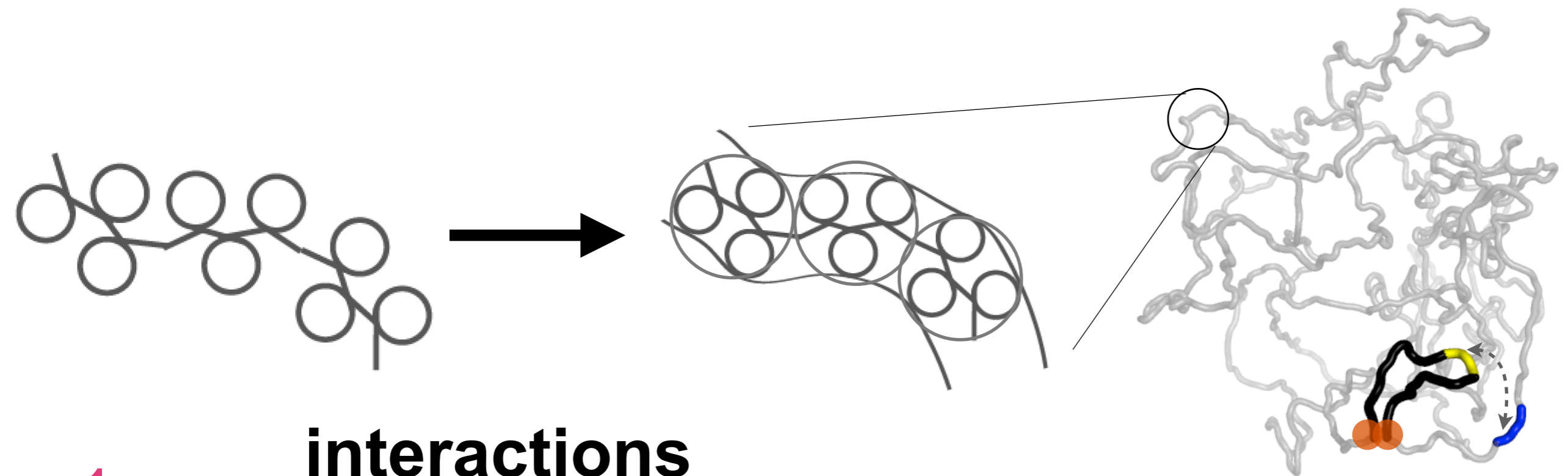
1



2

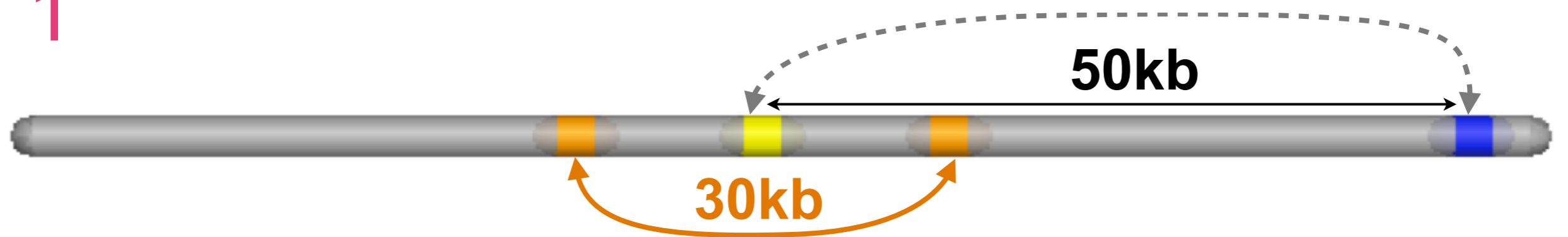


Model: chromatin as a polymer

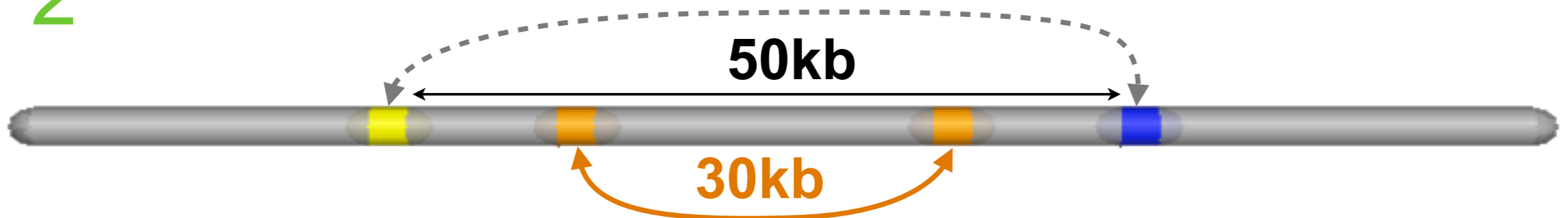


interactions

1



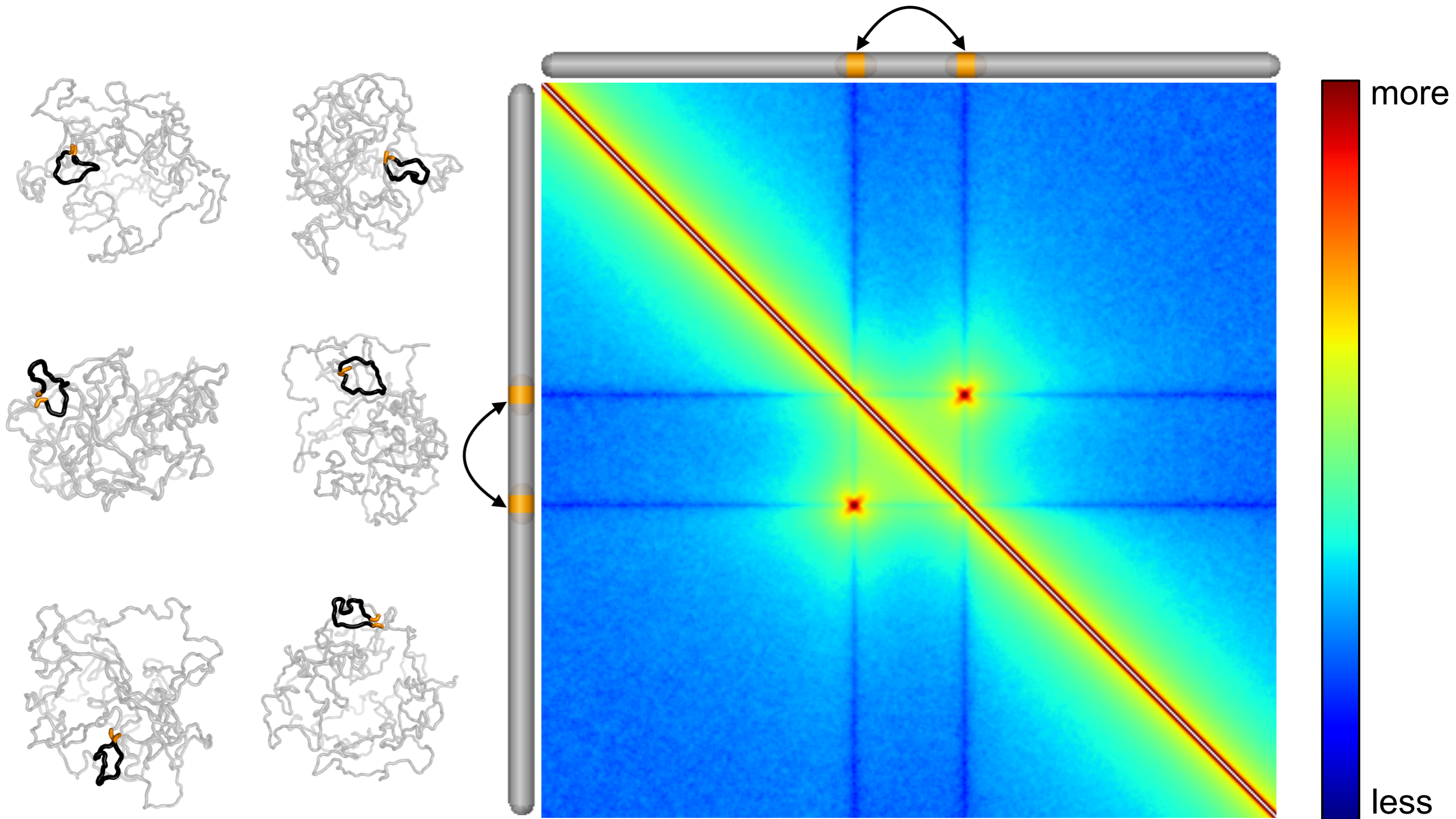
2



Langevin dynamics simulations

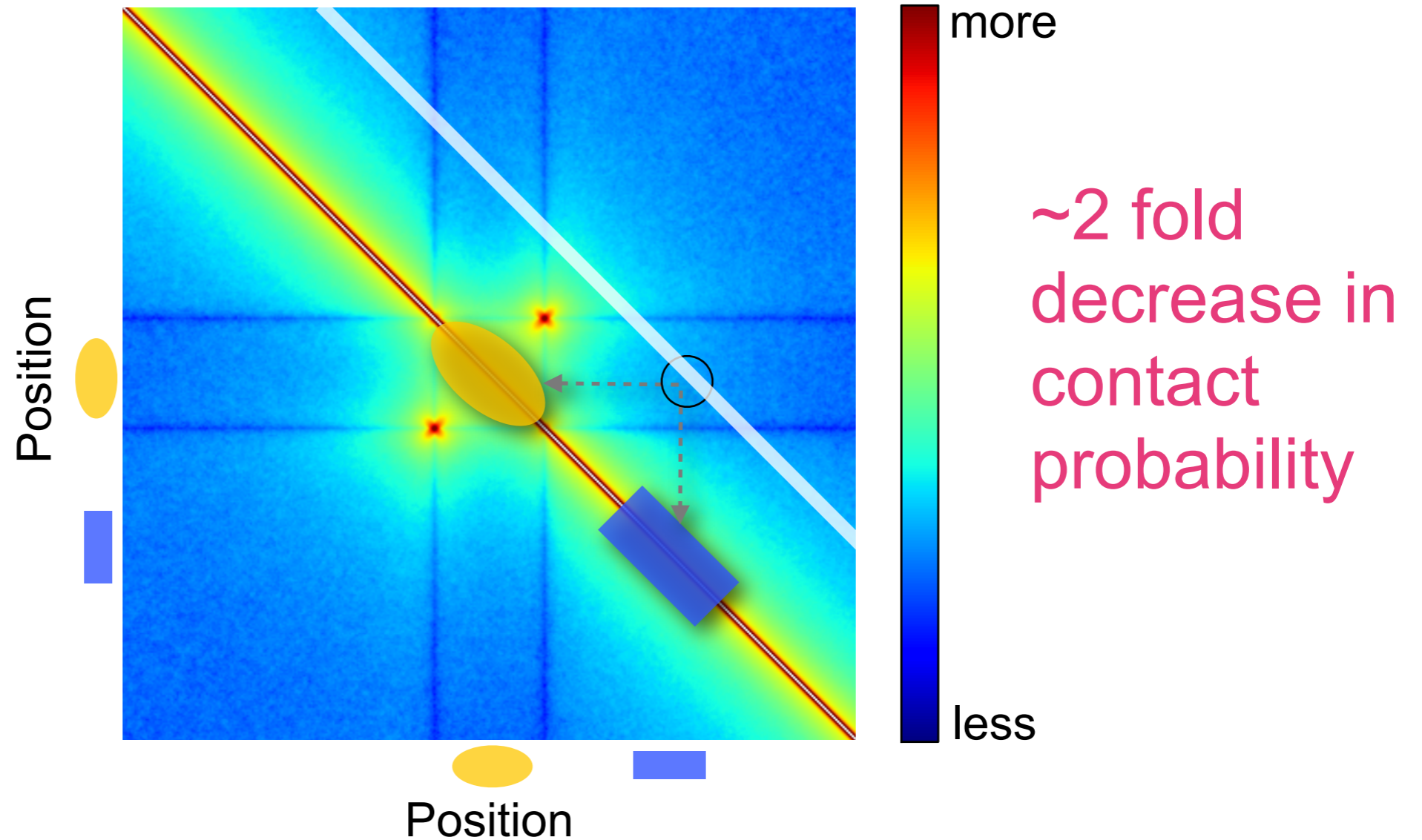
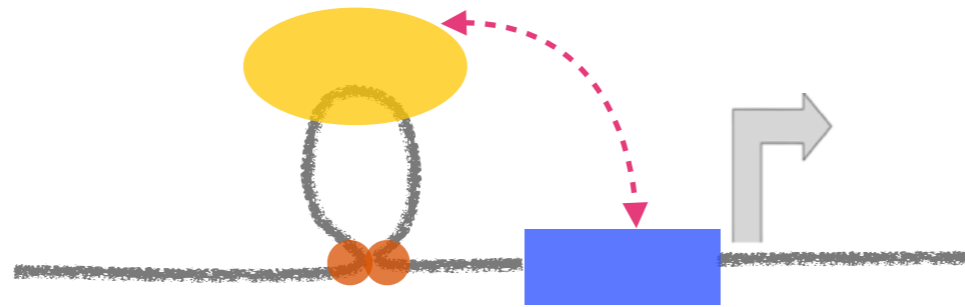
Results: Contact Maps

average over 10^5 conformations \longrightarrow 1 contact map

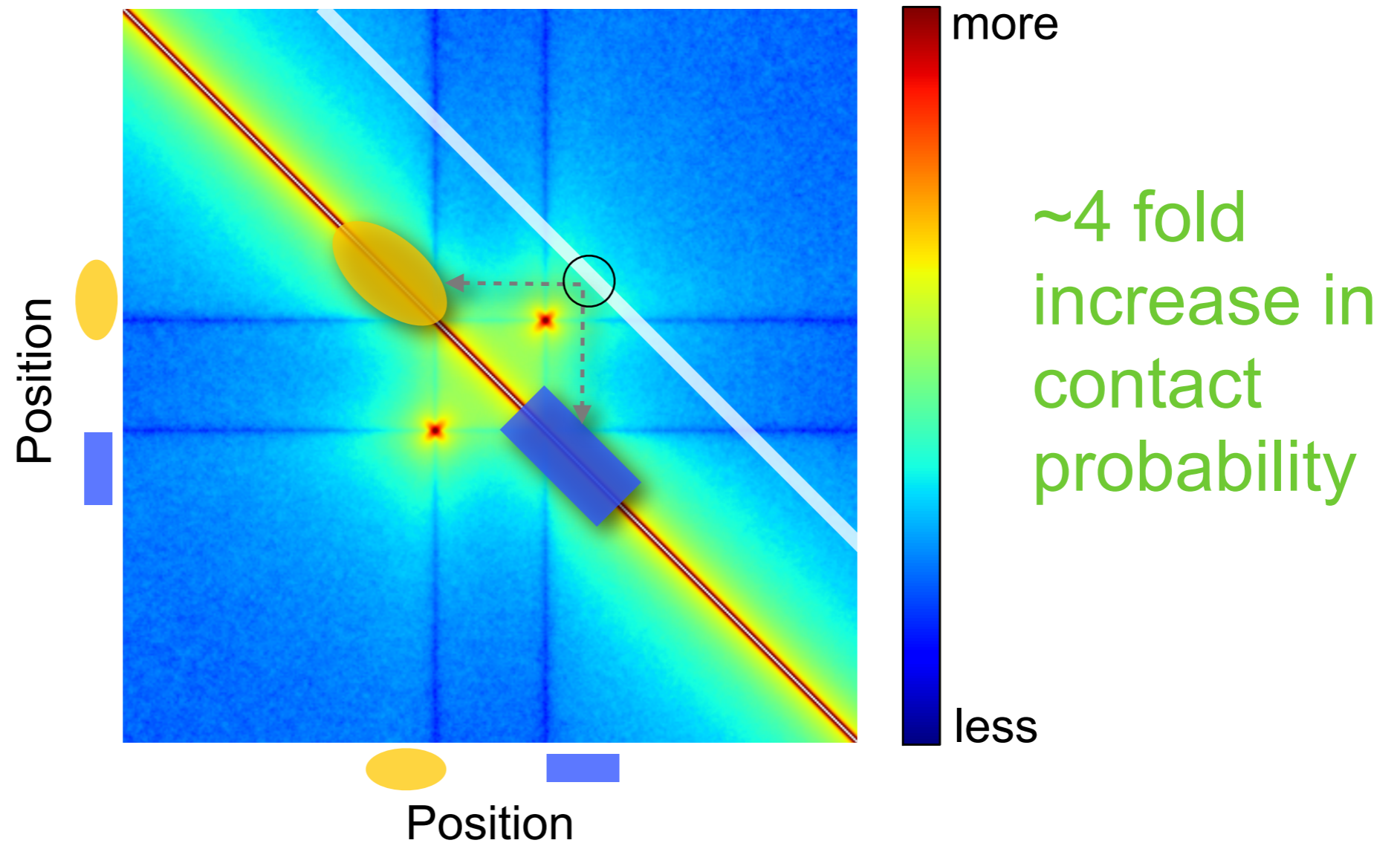
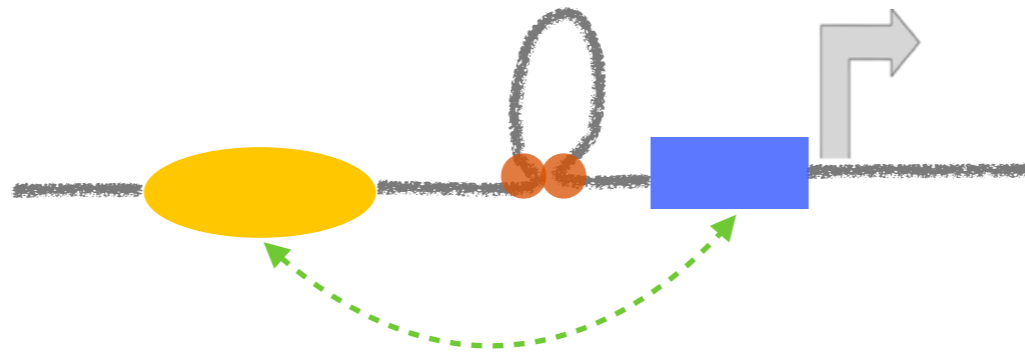


Case 1: Insulates

Enhancer inside loop. Promoter outside loop.

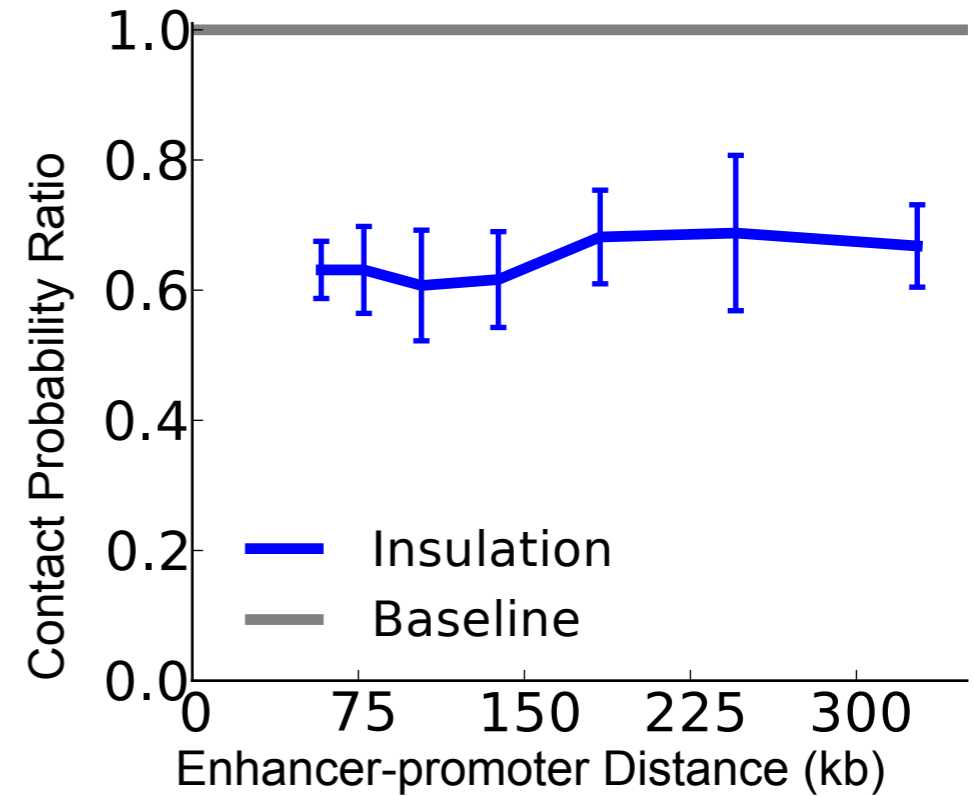
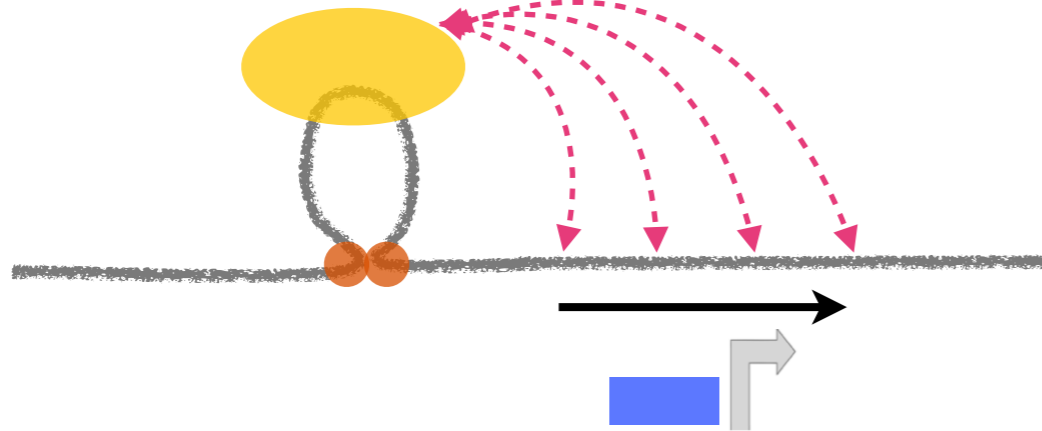


Case 2: Facilitates Enhancer before loop. Promoter after loop.

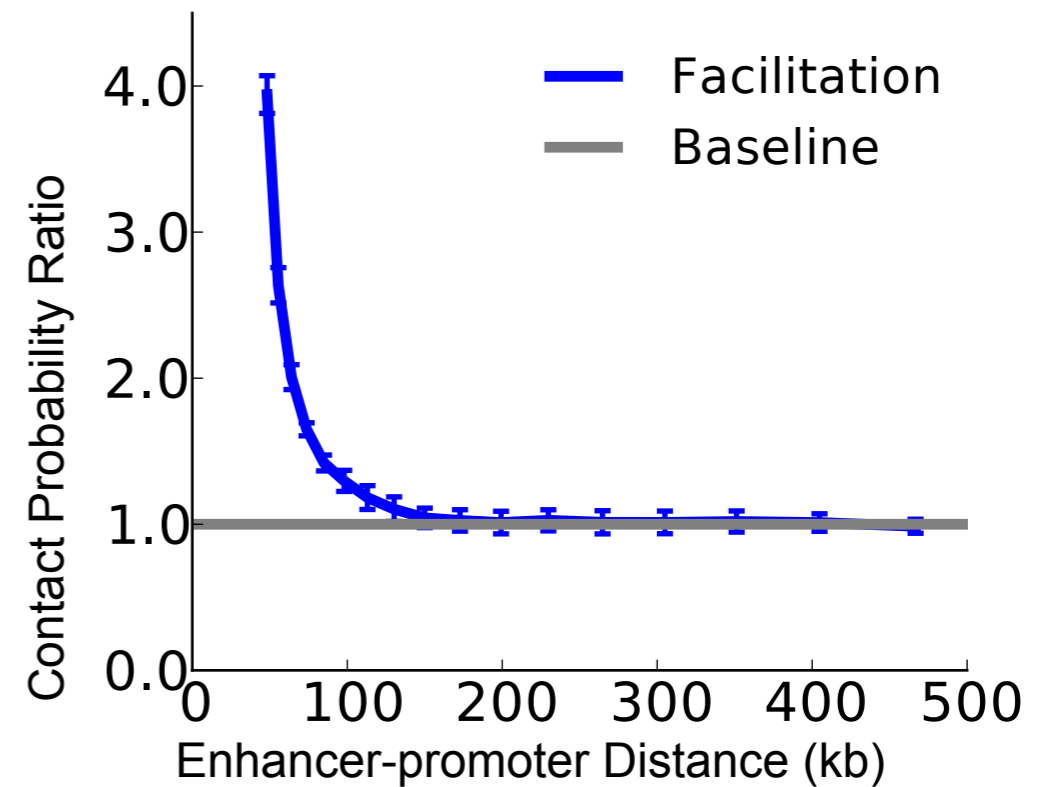
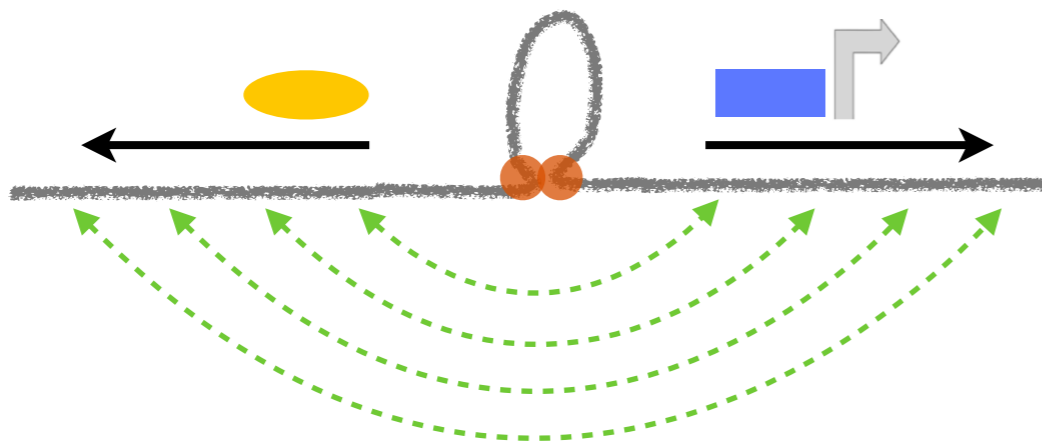


Insulation is global, while facilitation is local

1



2

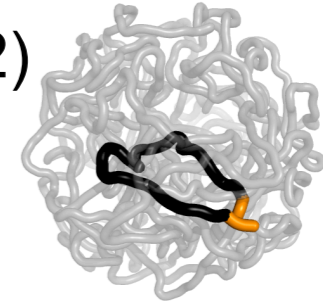


Weaker **insulation** and **facilitation** in compact chromatin

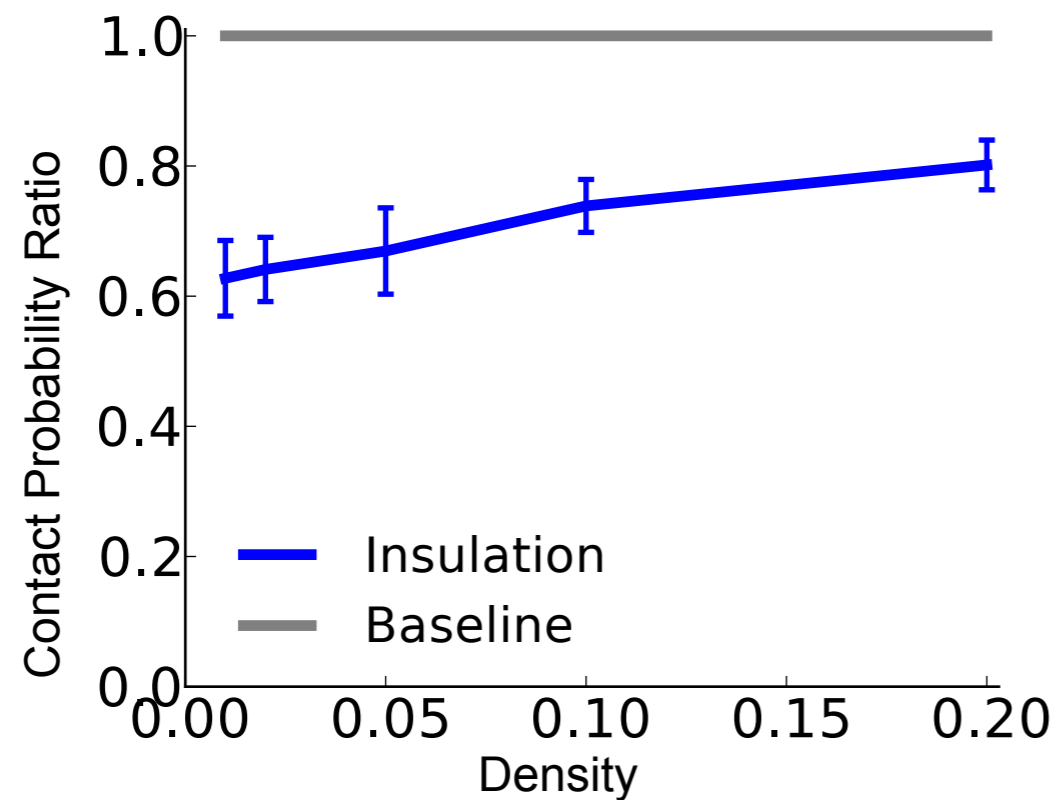
low density (0.01)



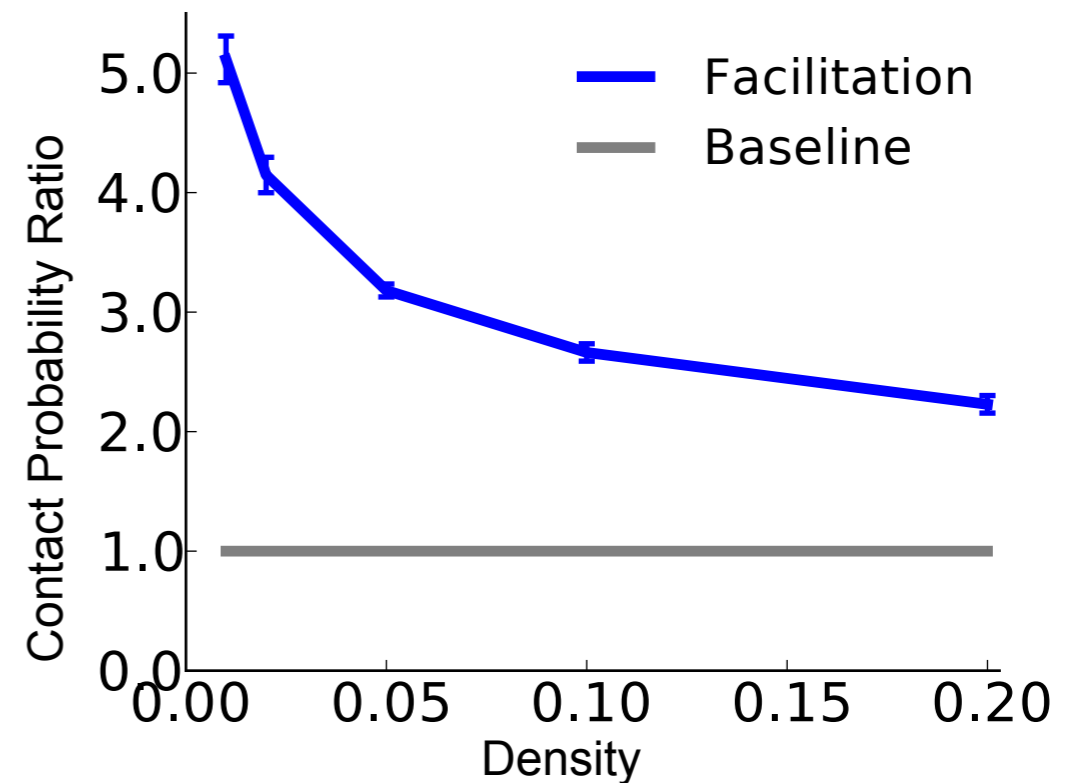
high density (0.2)



1



2



Similar **insulation** and **facilitation** regardless of topological constraints

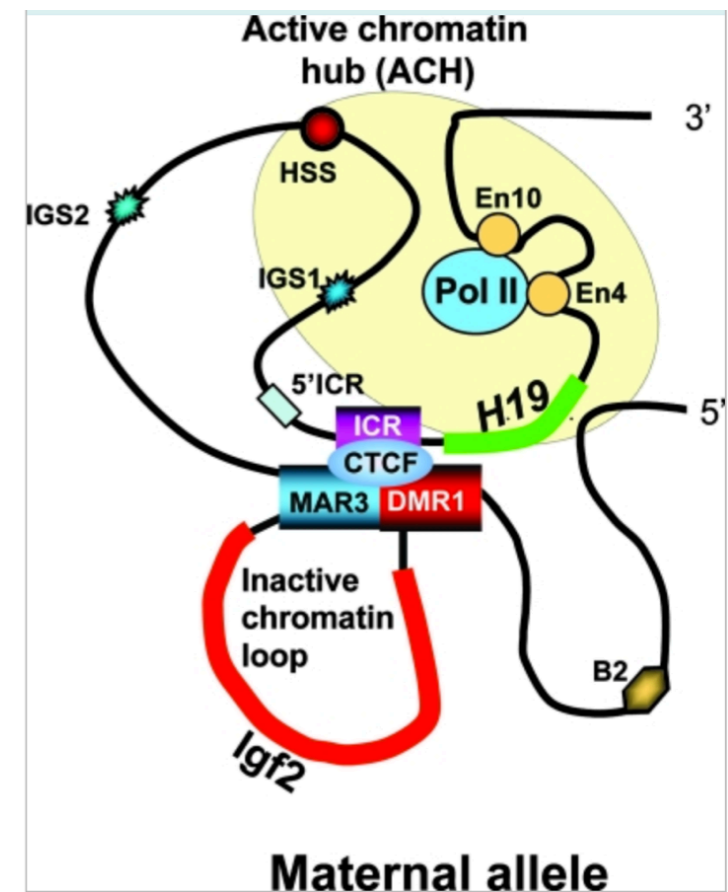
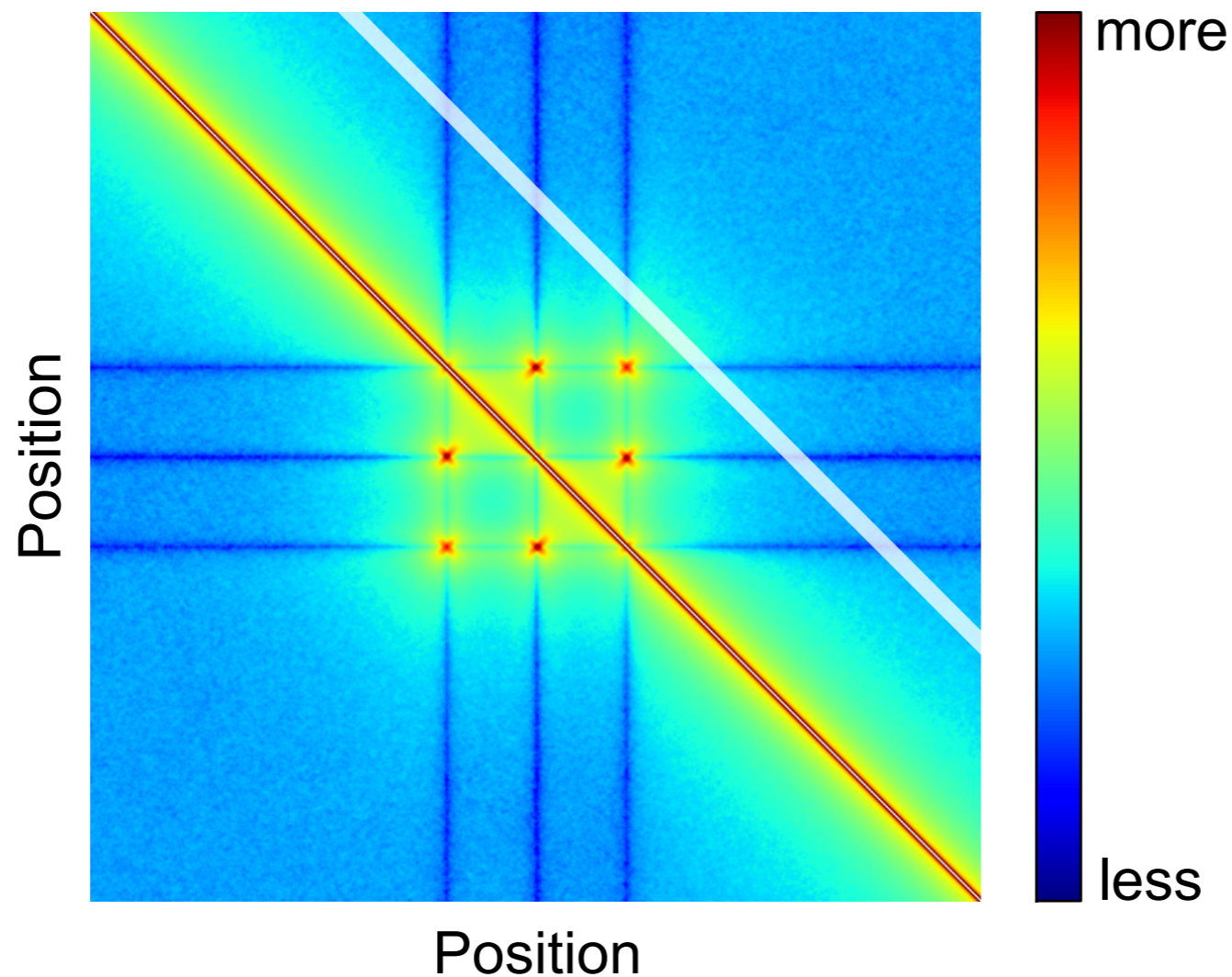
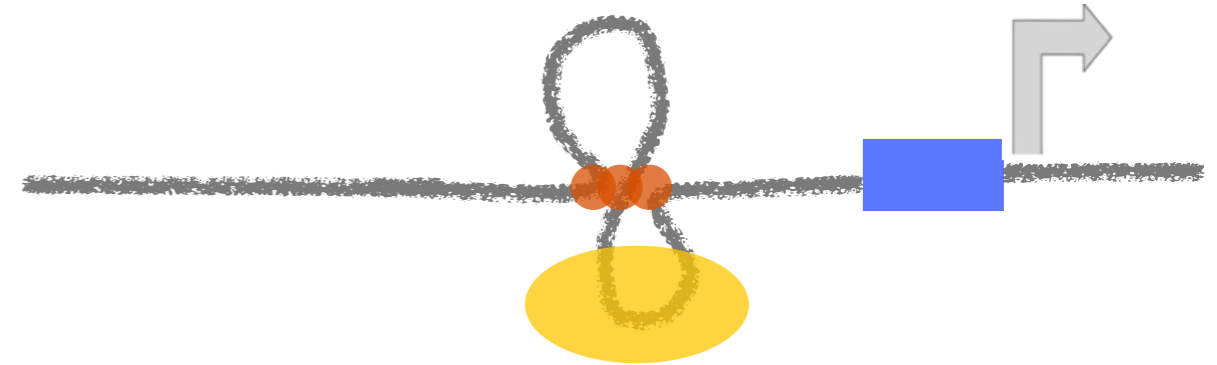
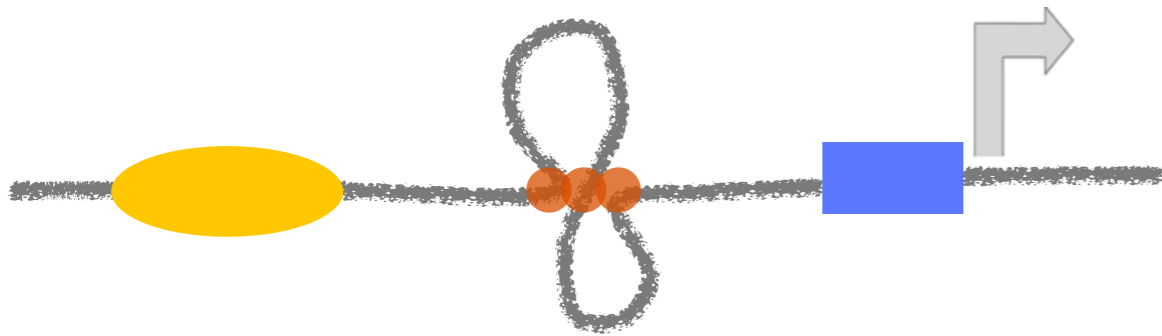
Without topological constraints = chain passing allowed



With topological constraints = chain passing not allowed

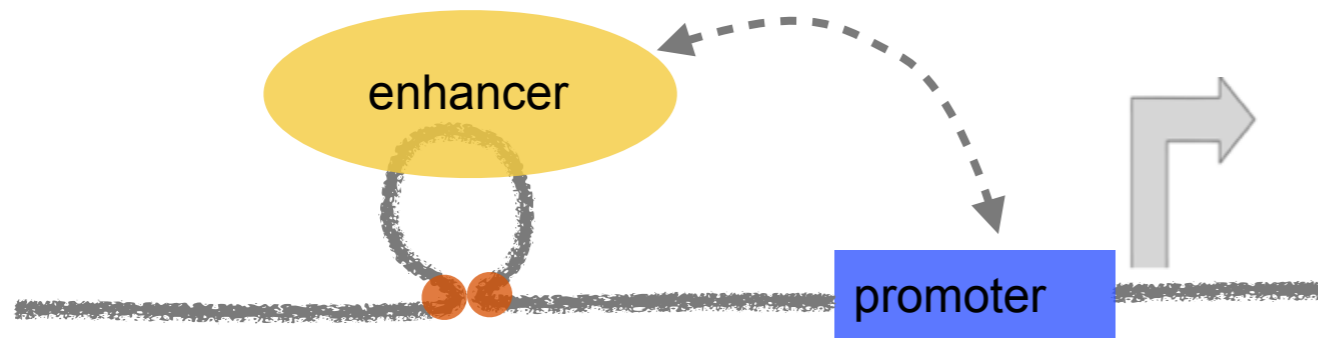


Insulation and facilitation are stronger for two loops elements



Part 1: Summary

1: Insulates: ~2 fold effect

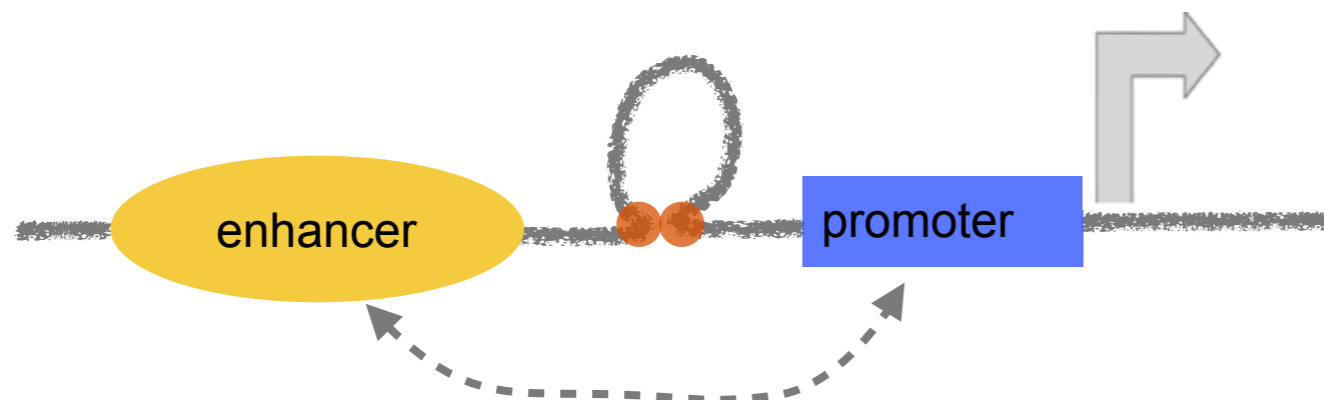


Insulation is constant as enhancer-promoter genomic distance increases.

Facilitation diminishes as enhancer-promoter genomic distance increases.

Weaker **insulation** and **facilitation** in compact chromatin.

2: Facilitates: ~4 fold effect



Similar **insulation** and **facilitation** with and without topological constraints.

Stronger **insulation** and **facilitation** with two consecutive loops.

Part 2: Fine scale analysis of experimental Hi-C contact maps

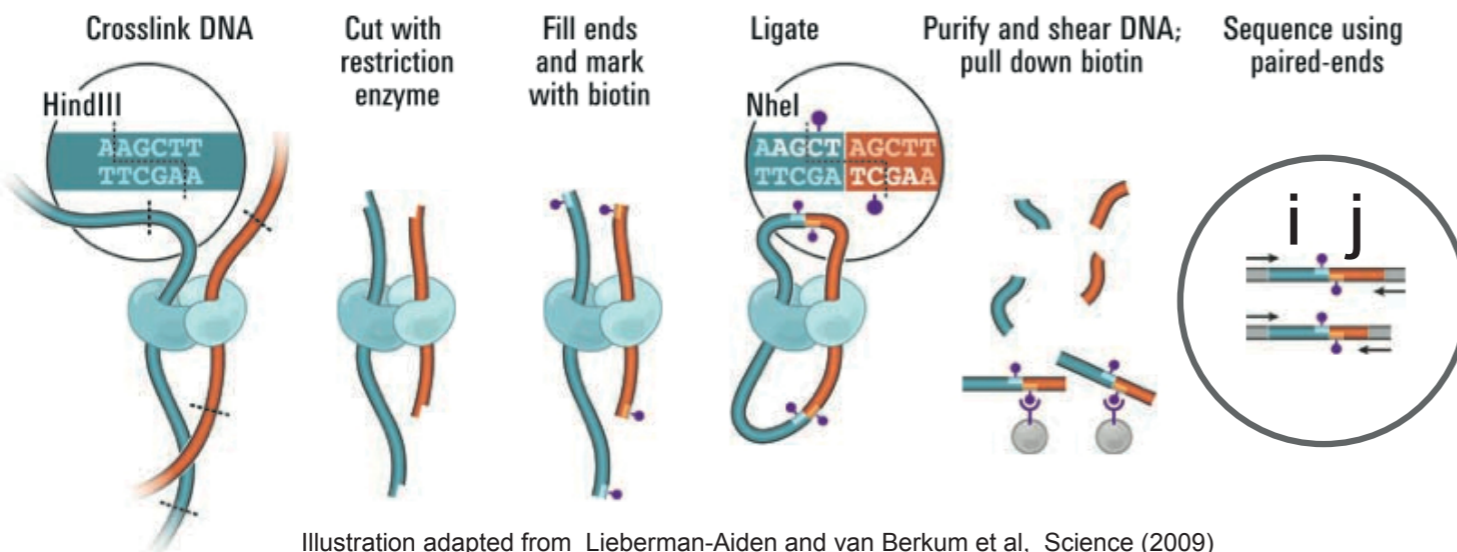
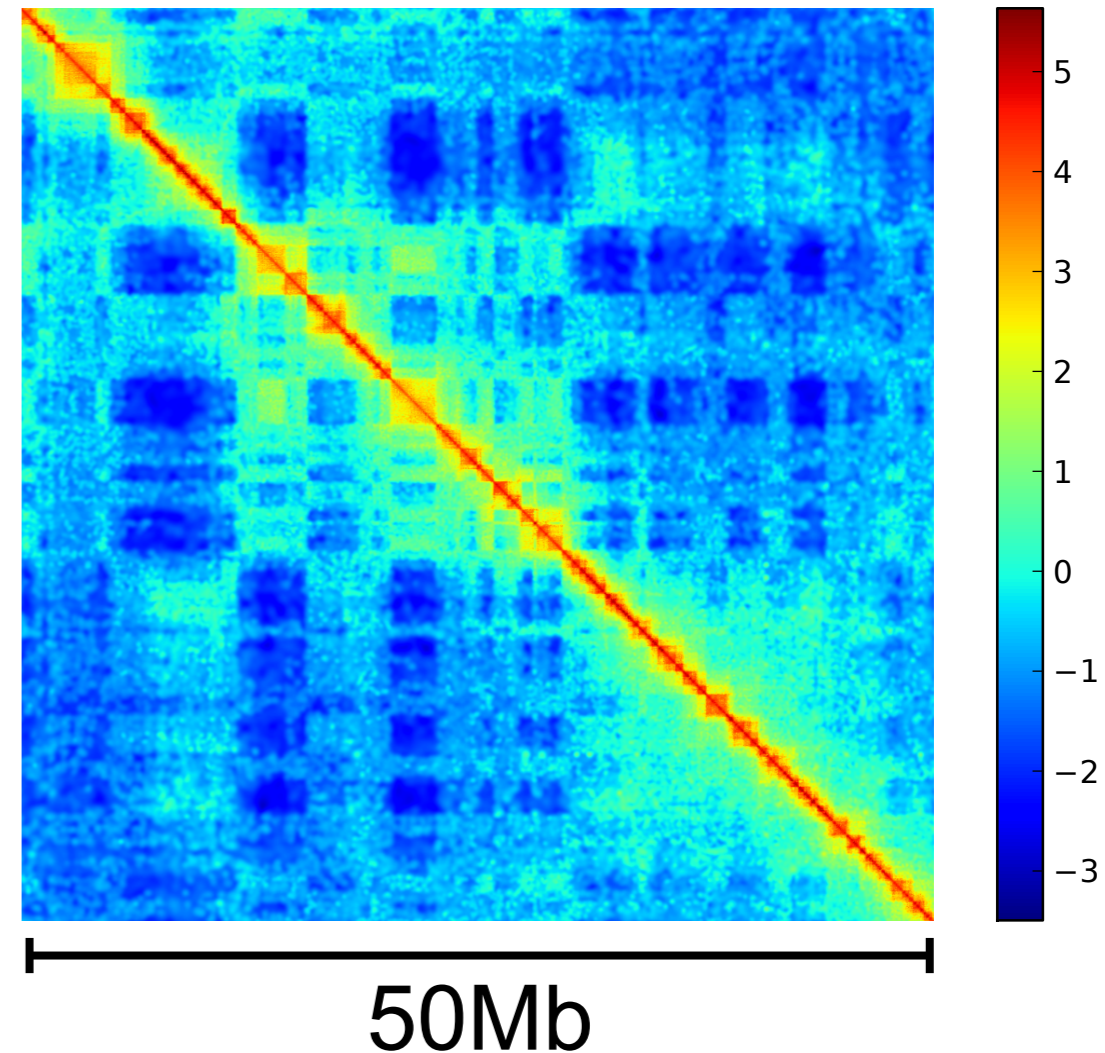


Illustration adapted from Lieberman-Aiden and van Berkum et al, Science (2009)

Hi-C experimentally measures spatial contacts in 3D

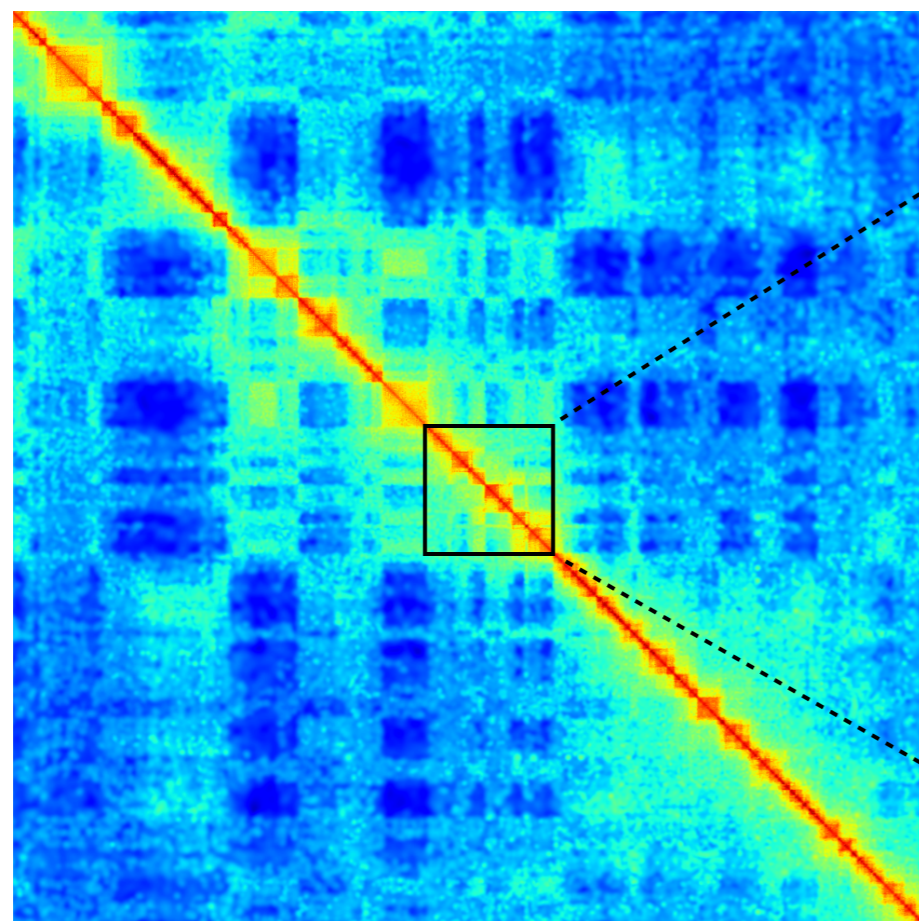
Region of chromosome 15



Topologically Associated Domains (TADs)

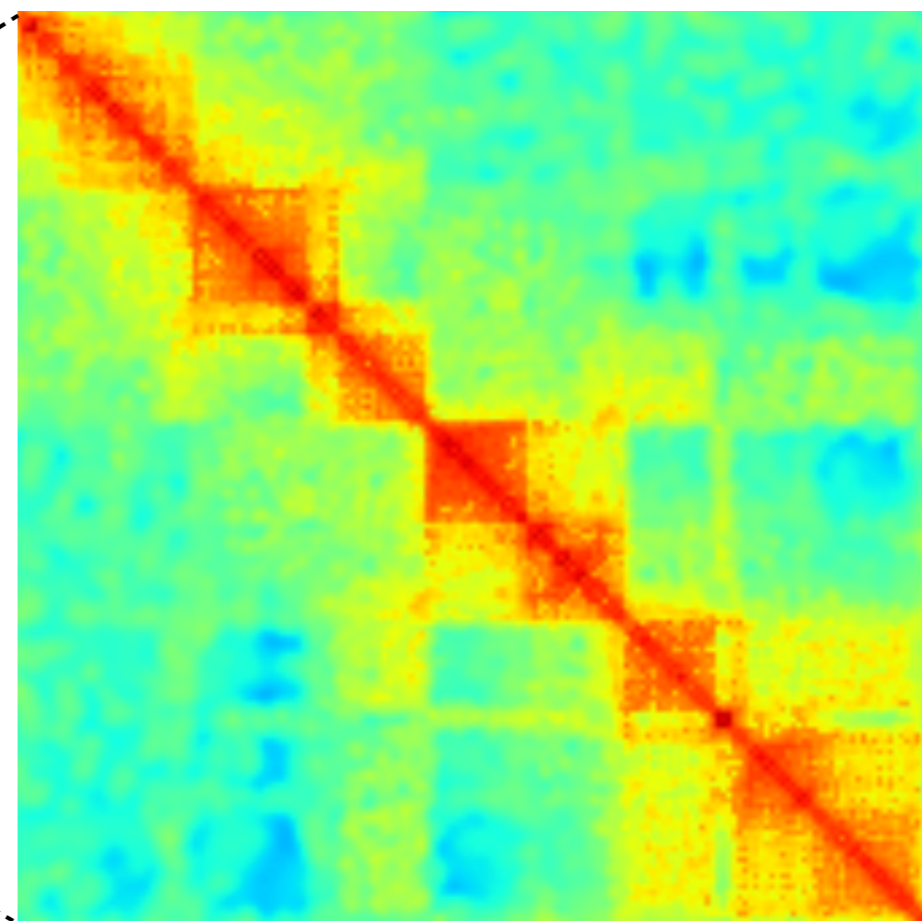
TAD size = 300 kb to 1Mb

Region of chromosome 15

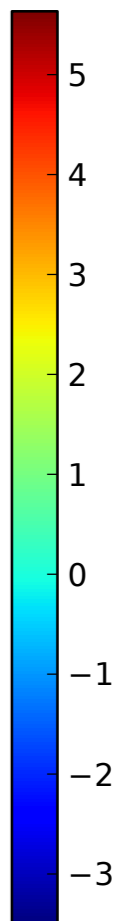


50Mb

Zoom in of chromosome 15

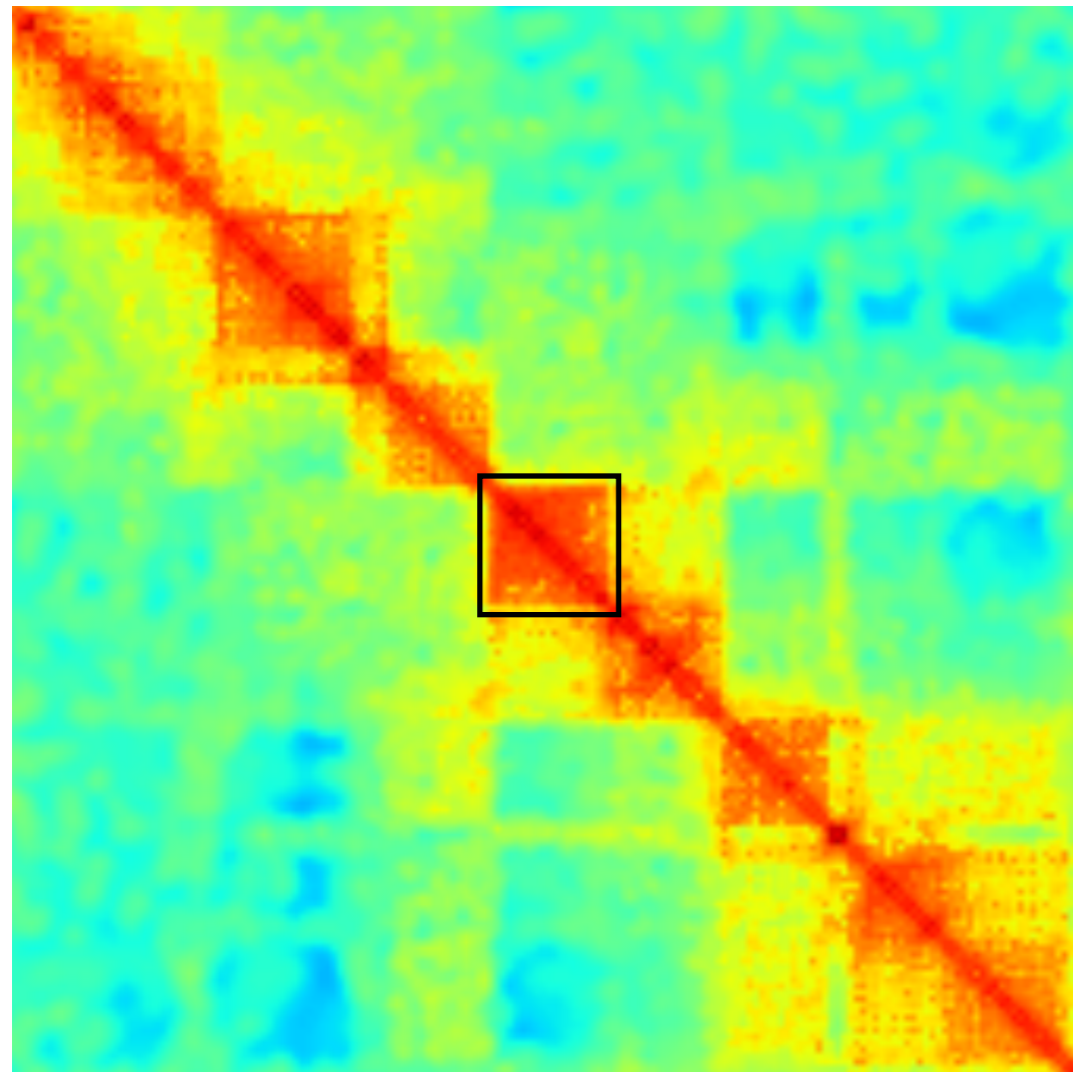


6.5Mb



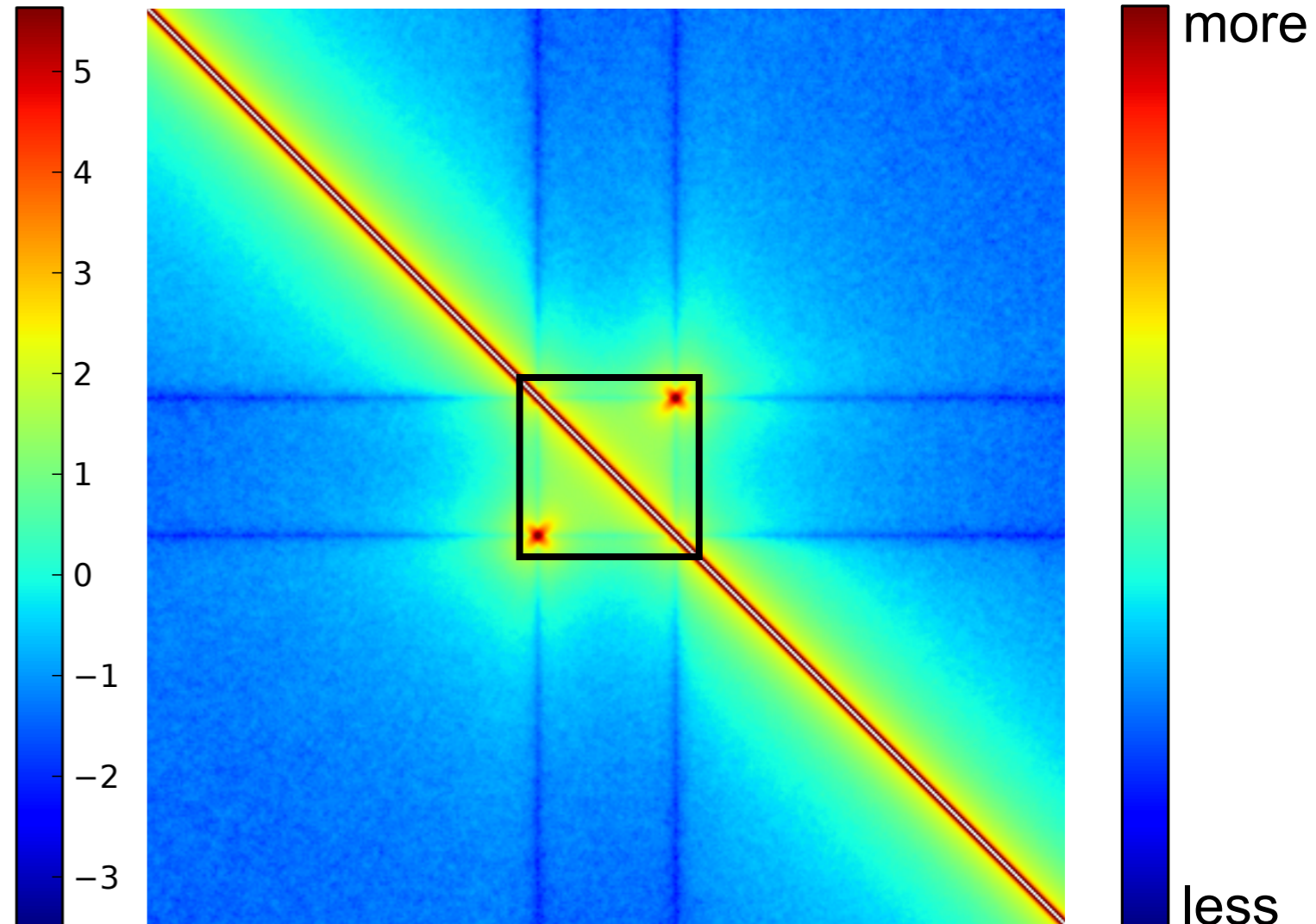
TADs are not single, static loops

Zoom in of chromosome 15



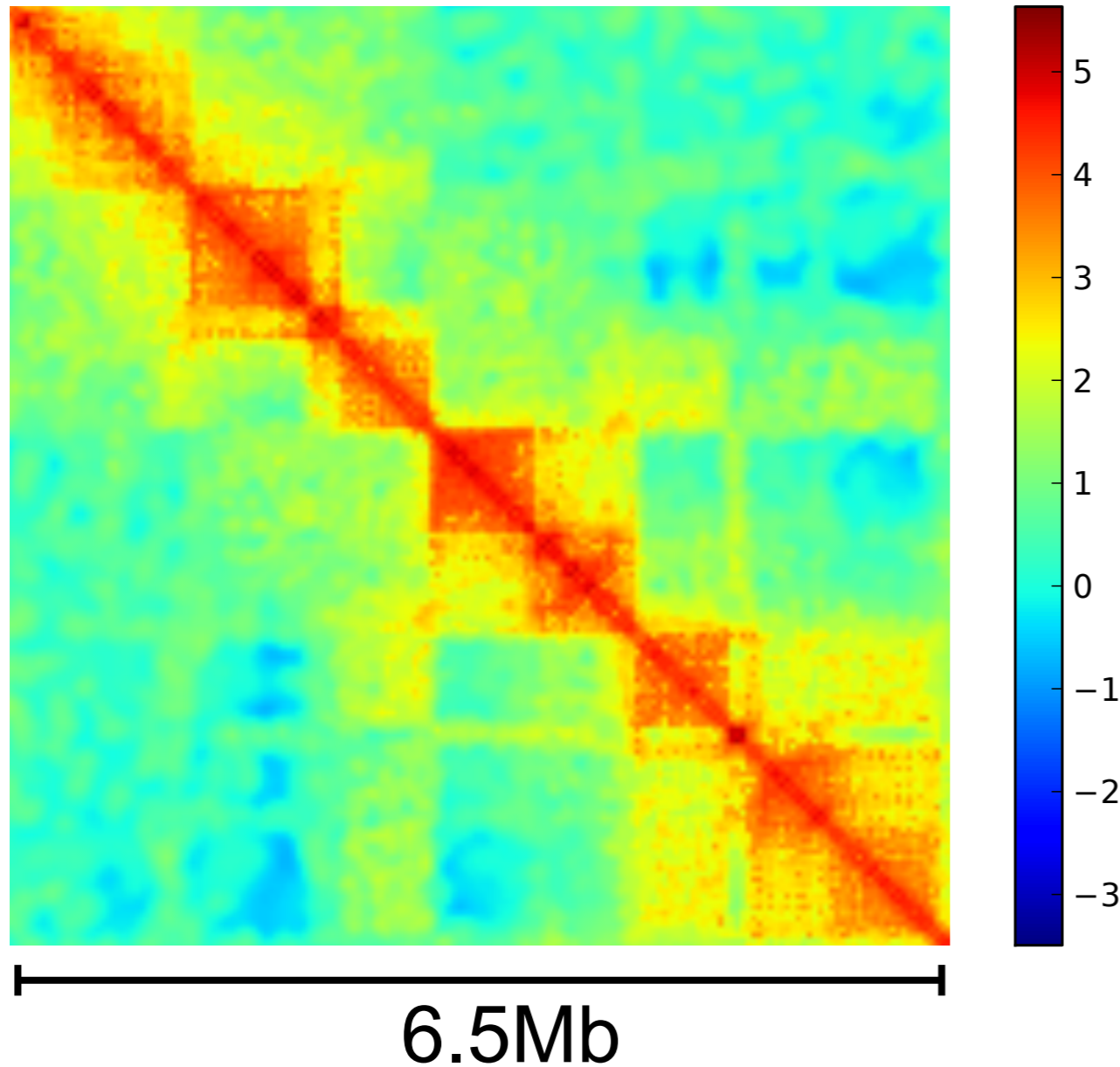
6.5Mb

Simulated polymer with loop



Before analyzing TADs, we need to find them: Automated TAD detection

Zoom in of chromosome 15



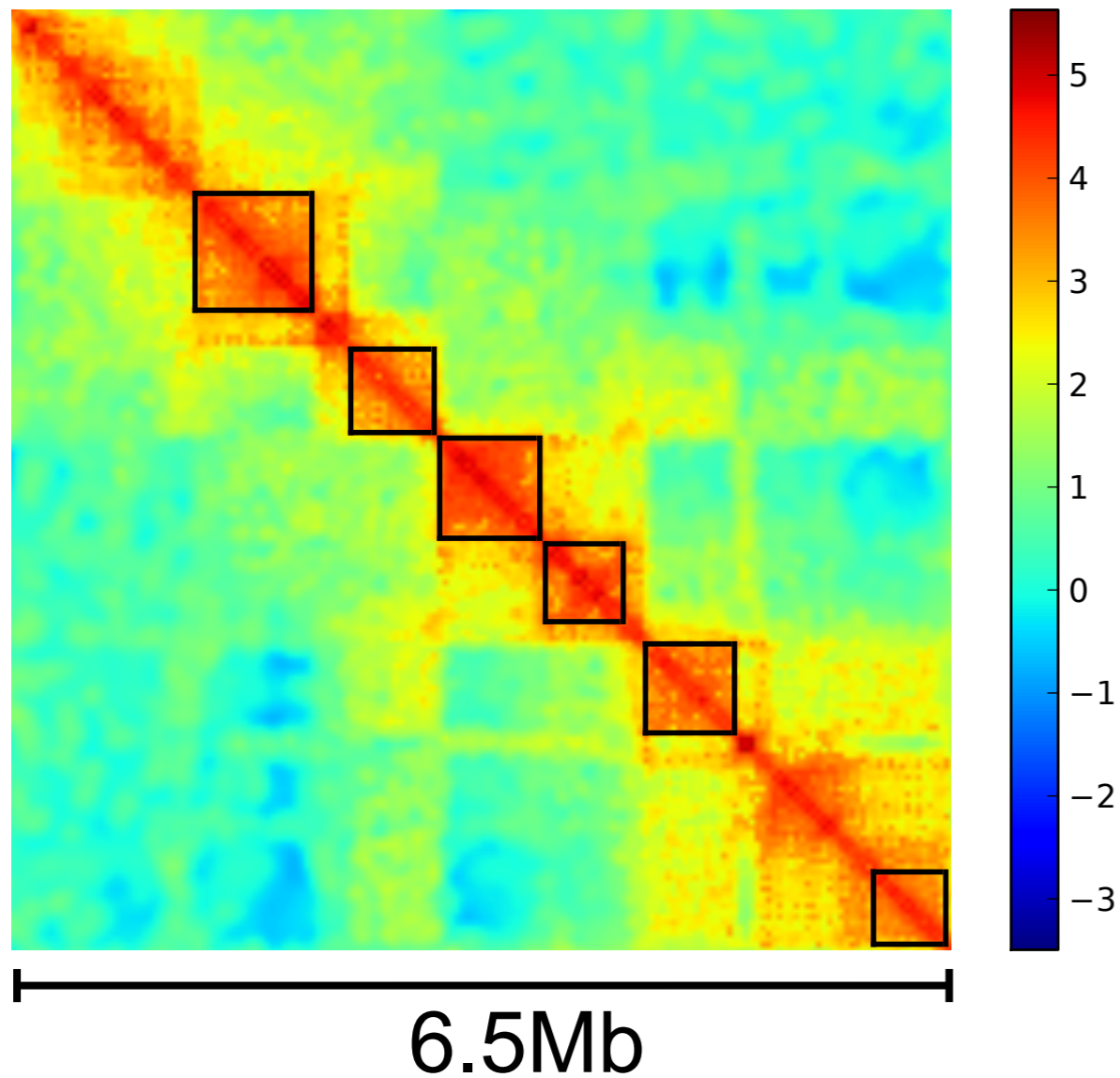
rather than detecting
TAD boundaries, we
detect enriched TAD
regions.

edge detection
sharp boundaries

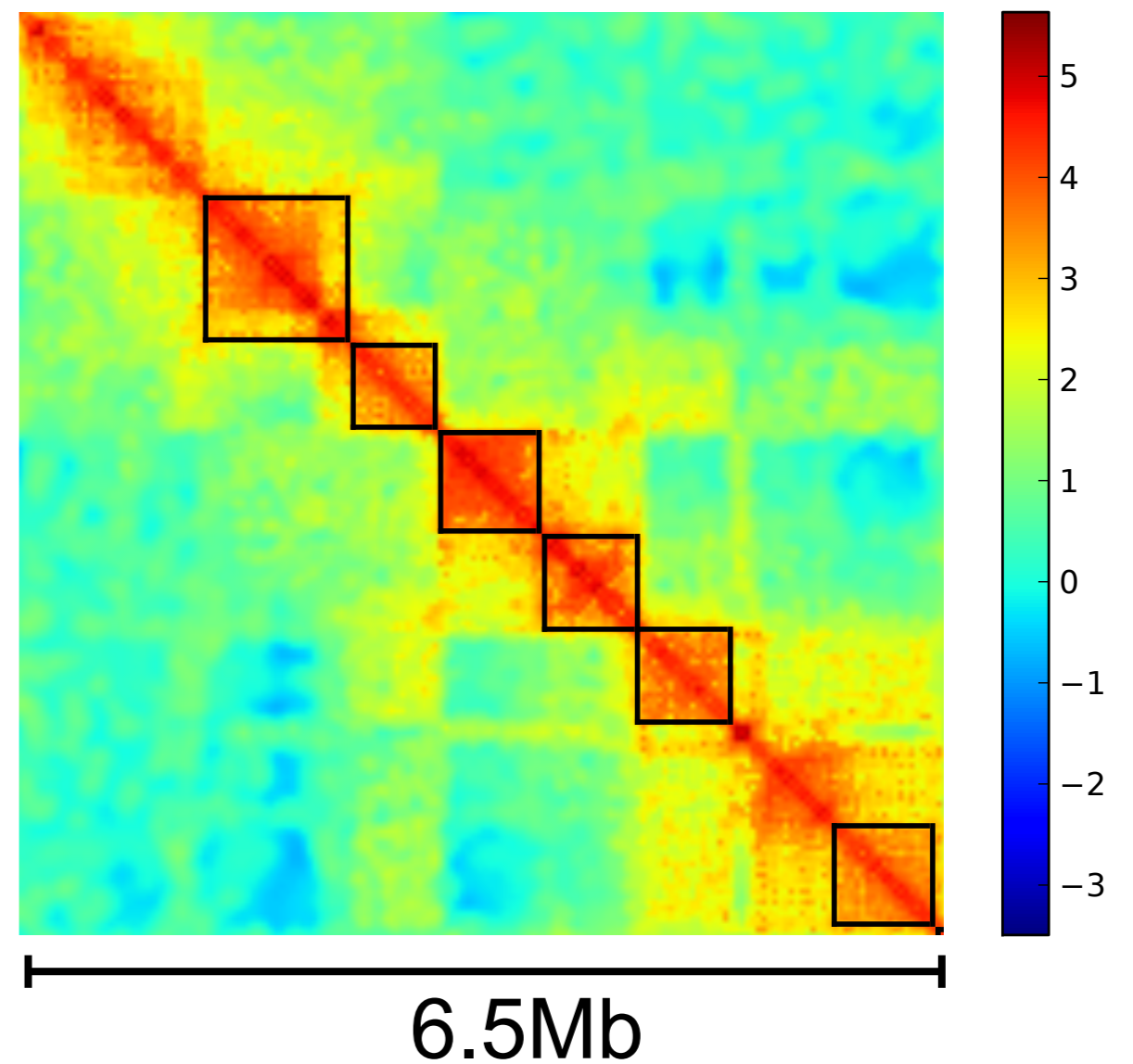
enriched mean

Automated TAD selection vs. manual TAD selection

Automated

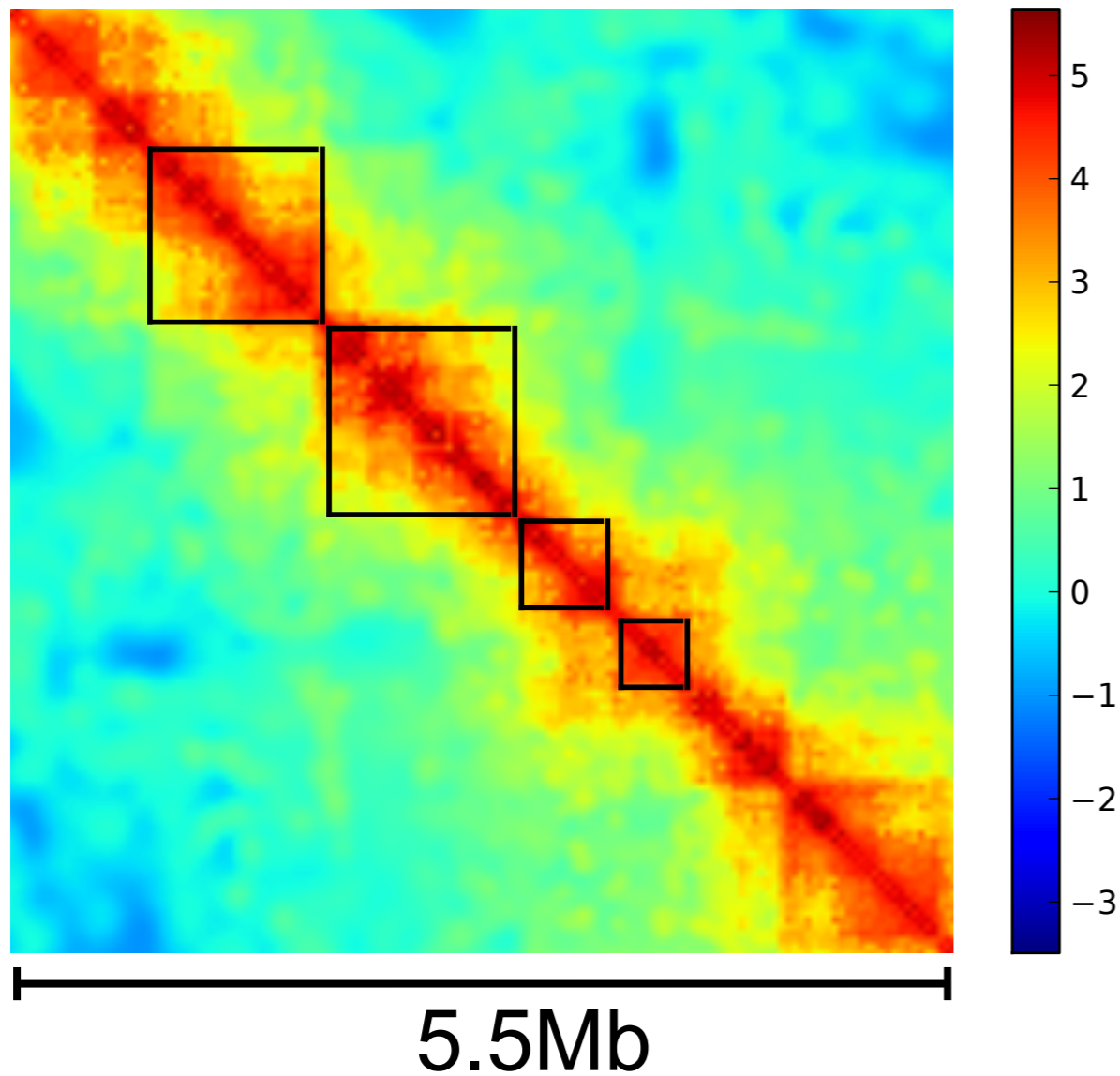


Manual

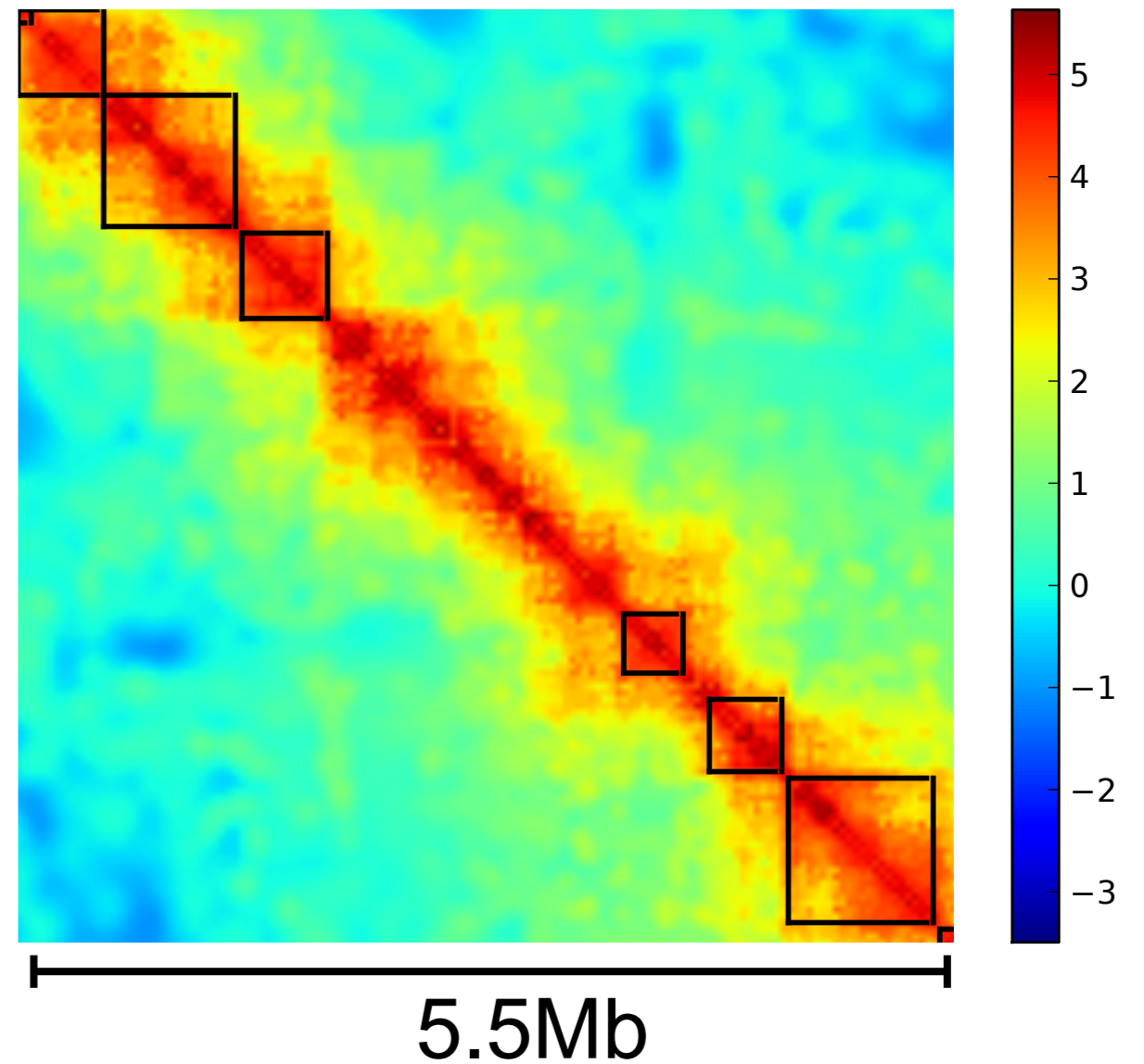


Automated TAD selection vs. manual TAD selection

Automated

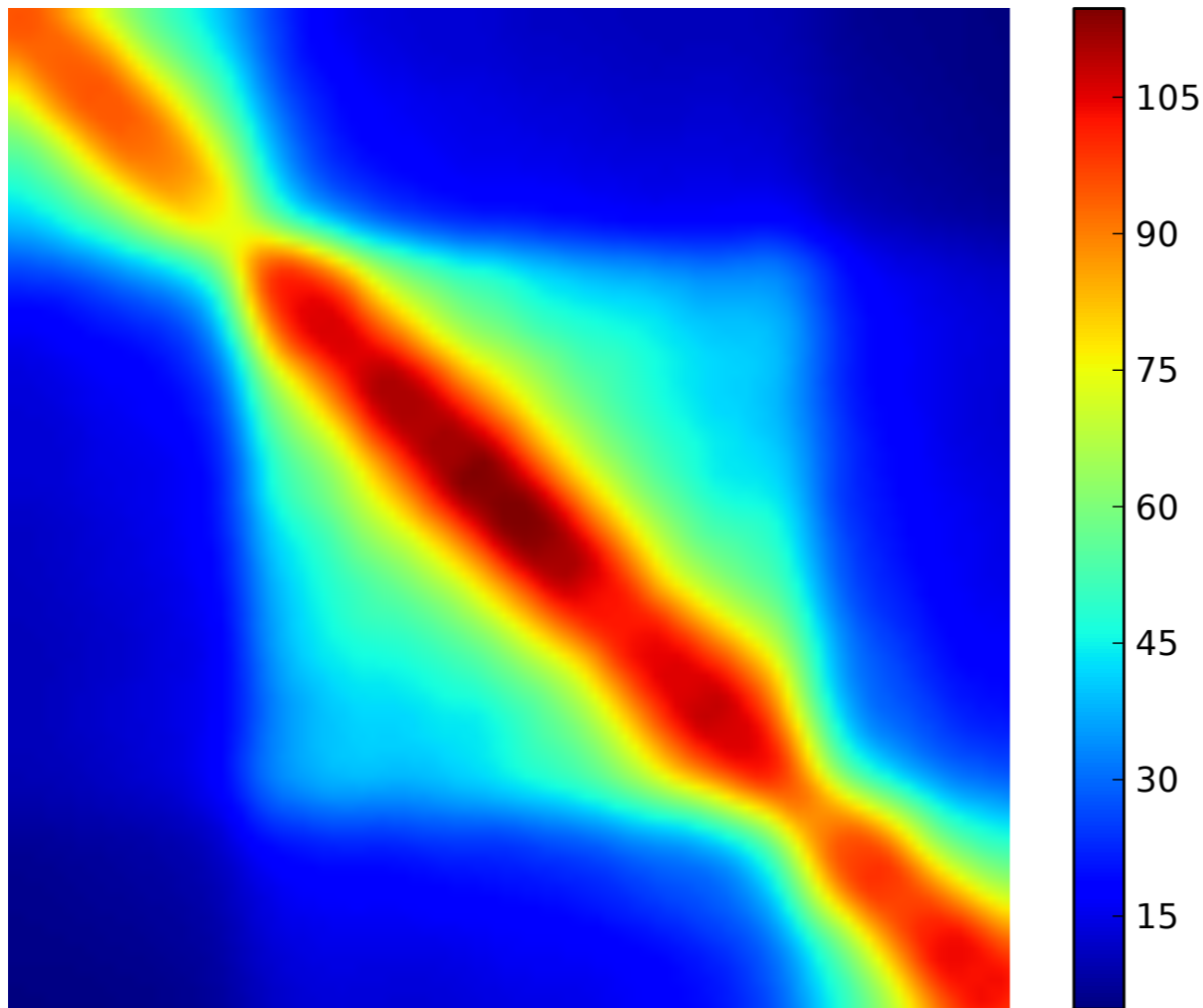


Manual

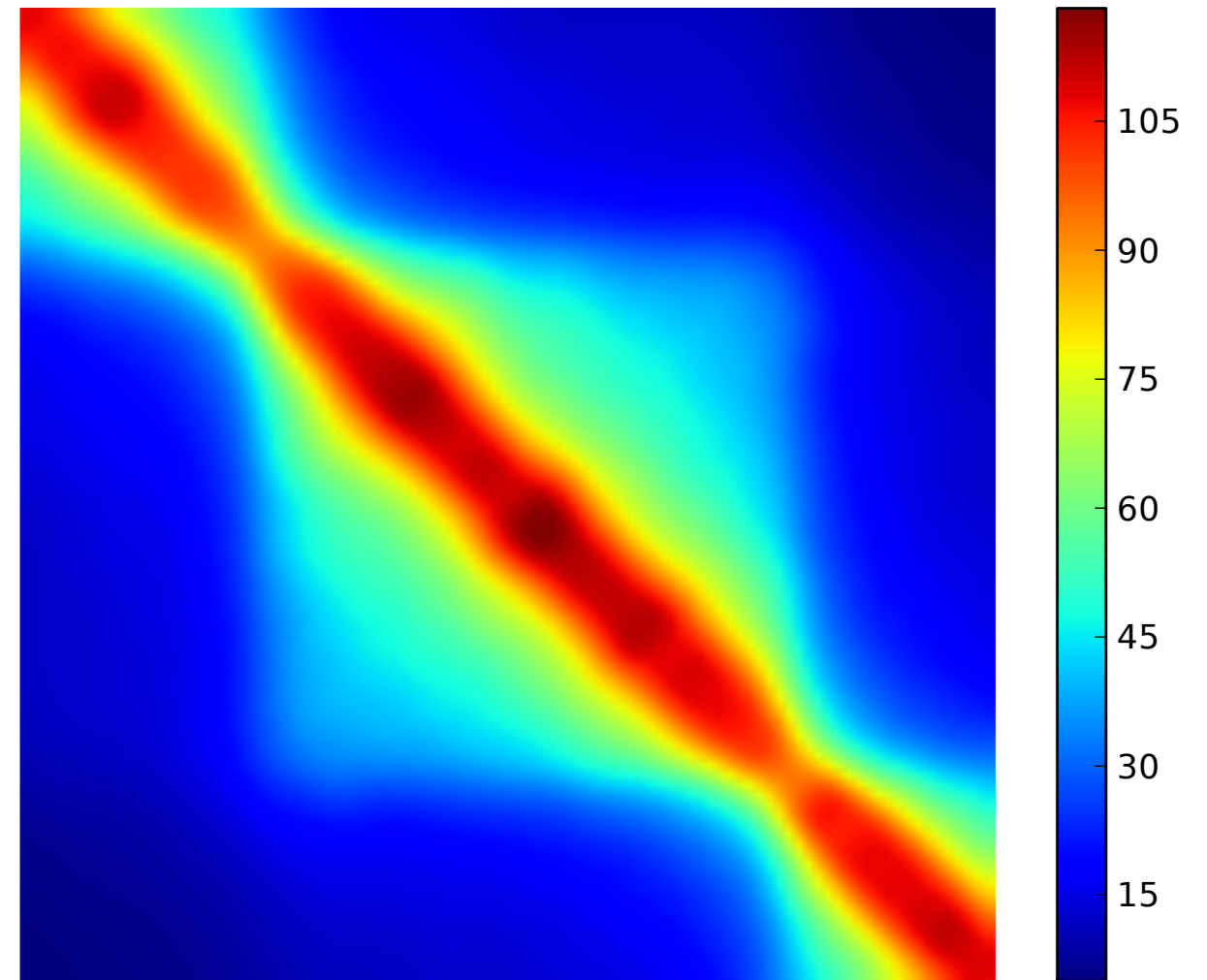


Average TAD for Chromosome 15

Automated



Manual



Acknowledgements



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*In mathematics you don't understand things, you just get used to them.
- John von Neumann*

Leonid Mirny lab:
Geoffrey Fudenberg
Maxim Imakaev

Pande lab: OpenMM Molecular dynamics software