Topology Seminar

Kyle Ormsby

of Reed College will be speaking on

The slice spectral sequence for the η -periodic motivic sphere

on October 21 at 3:15 in MIT Room 2-131

Infamously, the motivic Hopf map η is non-nilpotent, and the η -periodic motivic sphere spectrum detects this phenomenon. I will describe a slice-theoretic approach to this object, resulting in a computation of the E_2 -page of the η -periodic slice spectral sequence. This permits a complete computation of the homotopy groups of the η -periodic sphere when -1 is a sum of four squares in the base field. We also prove that, for a general field k, this spectral sequence is determined by the η -periodic slice spectral sequence over R. Some delicate convergence problems obstruct the final resolution of this problem, and the audience is invited to solve these. Our computations lead to a conjecture about the η -periodic sphere as a "connective Witt-theoretic *J*-spectrum," and also promise to help with slice computations of the motivic sphere. This is joint work with Oliver Röndigs.